



FEDERAL PUBLIC SERVICE COMMISSION
COMPETITIVE EXAMINATION FOR
RECRUITMENT TO POSTS IN BS-17
UNDER THE FEDERAL GOVERNMENT, 2014

Roll Number

APPLIED MATHEMATICS, PAPER-I

TIME ALLOWED:
THREE HOURS

MAXIMUM MARKS: 100

- NOTE: (i) Candidate must write **Q.No.** in the **Answer Book** in accordance with **Q.No.** in the **Q.Paper**.
(ii) Attempt **FIVE** questions in all by selecting **THREE** questions from **SECTION-A** and **TWO** questions from **SECTION-B**. **ALL** questions carry **EQUAL** marks.
(iii) No Page/Space be left blank between the answers. All the blank pages of Answer Book must be crossed.
(iv) Extra attempt of any question or any part of the attempted question will not be considered.
(v) **Use of Calculator is allowed.**

SECTION-A

- Q. No. 1.** (a) prove that $\text{curl}(w\vec{F}) = (\text{grad}w) \times \vec{F}$. If \vec{F} is irrotational and $w(x, y, z)$ is a scalar function. (10)
(b) Determine whether the line integral: (10)
$$\int_c (2xyz^2 dx + (x^2 z^2 + z \text{Cos} yz) dy + (2x^2 yz + y \text{Cos} yz) dz)$$
 is independent of the path of integration? If so, then compute it from $(1,0,1)$ to $(0, \frac{f}{2}, 1)$.
- Q. No. 2.** (a) State and prove Stoke's Theorem. (10)
(b) Verify Stoke's Theorem for the function $F = x^2 i - xy j$ integrated round the square in the plane $z=0$ and bounded by the lines $x = y = 0, x = y = a$. (10)
- Q. No. 3.** (a) Three forces act perpendicularly to the sides of a triangle at their middle points and are proportional to the sides. Prove that they are in equilibrium. (10)
(b) Three forces P, Q, R act along the sides BC, CA, AB respectively of a triangle ABC. Prove that, if $P \text{ Sec } A + Q \text{ Sec } B + R \text{ Sec } C = 0$, then the line of action of the resultant passes through the orthocentre of the triangle. (10)
- Q. No. 4.** (a) Find the centroid of the surface formed by the revolution of the cardioide $r = a(1 + \text{Cos } \theta)$ about the initial line. (10)
(b) A uniform ladder rests with its upper end against a smooth vertical wall and its foot on rough horizontal ground. Show that the force of friction at the ground is $\frac{1}{2} W \tan \theta$, where W is the weight of the ladder and θ is its inclination with the vertical. (10)
- Q. No. 5.** (a) Define briefly laws of friction give atleast one example of each law. (10)
(b) A uniform semi-circular wire hangs on a rough peg, the line joining its extremities making an angle of 45° with the horizontal. If it is just on the point of slipping, find the coefficient of friction between the wire and the peg. (10)

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SECTION-B

- Q. No. 6.** (a) If a point P moves with a velocity v given by $v^2 = n^2(ax^2 + 2bx + c)$, show that P executes a simple harmonic motion. Find the center, the amplitude and the time-period of the motion. (10)
- (b) A particle P moves in a plane in such a way that at any time t its distance from a fixed point O is $r = at + bt^2$ and the line connecting O and P makes an angle $\theta = ct^{\frac{3}{2}}$ with a fixed line OA. Find the radial and transverse components of the velocity and acceleration of the particle at $t = 1$. (10)
- Q. No. 7.** (a) A particle of mass m moves under the influence of the force $F = a(i \sin \dot{s}t + j \cos \dot{s}t)$. If the particle is initially at rest on the origin, prove that the work done upto time t is given by $\frac{a^2}{m\dot{s}^2}(1 - \cos \dot{s}t)$, and that the instantaneous power applied is $\frac{a^2}{m\dot{s}^2} \sin \dot{s}t$. (10)
- (b) A battleship is streaming ahead with speed V , and a gun is mounted on the battleship so as to point straight backwards, and is set at an angle of elevation α , if v_0 is the speed of projection relative to the gun, show that the range is $\frac{2v_0}{g} \sin \alpha (v_0 \cos \alpha - V)$. Also prove that the angle of elevation for maximum range is $\arccos \left(\frac{V - \sqrt{V^2 - 8v_0^2}}{4v_0} \right)$. (10)
- Q. No. 8.** (a) Show that the law of force towards the pole, of a particle describing the curve $r^n = a^n \cos n\theta$ is given by $f = \frac{(n+1)h^2 a^{2n}}{r^{2n+3}}$. (10)
- (b) A bar 2 ft. long of mass 10 lb., lies on a smooth horizontal table. It is struck horizontally at a distance of 6 inches from one end, the blow being perpendicular to the bar. The magnitude of the blow is such that it would impart a velocity of 3 ft./sec. to a mass of 2 lb. Find the velocities of the ends of the bar just after it is struck. (10)
